

a)

$$\Pi_1 = \{ n^2 \mid n \in \mathbb{N} \wedge n^2 < 50 \}$$

$$\Pi_2 = \{ n \mid n \in \mathbb{N} \wedge 10 < n < 20 \wedge (n \text{ ist ungerade}) \}$$

$$\Pi_3 = \{ xyz \mid x, y, z \in \{ 1, 2, \dots, 8, 9 \} \}$$

$$\Pi_4 = \{ (\text{Vorspeise, Hauptgang, Dessert}) \mid \text{Vorspeise} = \text{Suppe}, \\ \text{Hauptgang} \in \{ \text{Fisch, Huhn, Tofu} \}, \text{Dessert} \in \{ \text{Eis, Pudding} \} \}$$

$$\Pi_5 = \{ D \mid D \subseteq \{ \text{Ananassaft, Baileys, Orangensaft, Rum, Wodka} \} \}$$

b)

$$|\Pi_1| = 8 \quad (\text{weil } 0^2, 1^2, 2^2, \dots, 7^2 \text{ kleiner als } 50 \text{ sind})$$

$$|\Pi_2| = 5 \quad (\text{weil es } 11, 13, 15, 17, 19)$$

$$|\Pi_3| = 729 \quad (\text{weil } 9^3 = 729)$$

$$|\Pi_4| = 18 \quad (\text{weil } 2^* 3, 3 = 18)$$

$$|\Pi_5| = 6 \quad (\text{weil es } 6 \text{ verschiedene Getränke gibt})$$

c/

$$\Pi_1 = \{0, 1, 4, 9, 16, 25, 36, 49\}$$

$$\Pi_2 = \{11, 13, 15, 17, 19\}$$

$$\Pi_3 = \{123, 222, 999, \dots\}$$

$$\Pi_4 = \{(Suppe, Fisch, Eis), (Suppe, Huhn, Eis), \\ (Suppe, Tofu, Eis), \dots\}$$

$$\Pi_5 = \{\{\}, \{Baileys\}, \{Coca\}, \dots\}$$